

DPP No. 26

Total Marks : 27

Max. Time : 30 min.

Topics :	Method of Differentiation, Straight Line, Continuity & Derivability, Circle
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Type of Questions	M.M.,	, Min.	
Comprehension (no negative marking) Q.1 to Q.2	(3 marks, 3 min.)	[6,	6]
Single choice Objective (no negative marking) Q.3,4,5	(3 marks, 3 min.)	[9,	9]
Subjective Questions (no negative marking) Q.6,7,8	(4 marks, 5 min.)	[12,	15]

COMPREHENSION (1 - 2)

In calculus the derivative of any function y = f(x) is defined as

$$D f(x) = \lim_{h \to 0} \frac{f(x+h) - f(x)}{h}$$

Now instead of this usual definition of derivative Df(x), define a new kind of derivative $D^*f(x)$, which can be calculated by the formula

$$D^{*} f(x) = \lim_{h \to 0} \frac{f^{2}(x+h) - f^{2}(x)}{h}$$

where f² (x) = (f(x))².

1. If
$$f(x) = \frac{x}{\ell n x}$$
, then D* $f(x)$ is

(A) $\frac{\ell n x - 1}{(\ell n x)^2}$ (B) $\frac{2x(\ell n x - 1)}{(\ell n x)}$ (C) $\frac{2x(\ell n x - 1)}{(\ell n x)^2}$ (D) $\frac{2x(\ell n x - 1)}{(\ell n x)^3}$

2. If function $g(x) = x^x$, then $D^* g(x) |_{x=1}$ is (A) 1 (B) $2e^e$ (C) 2 (D) not defined

3.The point ([P + 1], [P]) lies inside the circle $x^2 + y^2 - 2x - 15 = 0$, then set of all values of P is
(where [.] represents greatest integer function)
(A) [-2, 3)(B) (-2, 3)(C) [-2, 0) \cup (0, 3)(D) [0, 3)

4. The line L given by $\frac{x}{5} + \frac{y}{b} = 1$ passes through the point (13, 32). The line K is parallel to L and has the

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equation $\frac{x}{c} + \frac{y}{3} = 1$. Then the distance between L and K is

(A)
$$\sqrt{17}$$
 (B) $\frac{17}{\sqrt{15}}$ (C) $\frac{23}{\sqrt{17}}$ (D) $\frac{23}{\sqrt{15}}$

- 5. If the normal to differentiable curve y = f(x) at x = 0 be given by the equation 3x y + 3 = 0, then the value
 - of $\lim_{x\to 0} \frac{x^2}{f(x^2) 5f(4x^2) + 4f(7x^2)}$ is (A) 1/3 (B) - 1/3 (C) - 1/5 (D) 1/4
- 6. A triangle has two of its sides along the lines $y = m_1 x \& y = m_2 x$, where m_1 , m_2 are the roots of the equation $3x^2 + 10x + 1 = 0$. If H (6, 2) be the orthocentre of the triangle, find the equation of the third side of the triangle.

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7.
$$f(x)$$
 is defined as under : $f(x) = \begin{cases} ax(x-1)+b ; & x < 1 \\ x-1 ; & 1 \le x \le 3 \\ cx^2 + dx + 2 ; & x > 3 \end{cases}$

Determine the constants a, b, c and d, given that

- (i) f(x) is continuous for all x
- (ii) f'(1) does not exist
- (iii) f'(x) is continuous at x = 3

8. Let f(x) be a function of x defined as
$$f(x) = \begin{cases} \frac{x^2 - 1}{x^2 - 2|x - 1| - 1} & , & x \neq 1 \\ \frac{1}{2} & , & x = 1 \end{cases}$$

Discuss the continuity of function at x = 1.

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Answers Key

- **1.** (D) **2.** (C) **3.** (A) **4.** (C)
- **5.** (B) **6.** 3x + y + 1 = 0
- 7. $a \neq 1$, b = 0, c = 1/3, d = -1

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